### **Comparison of Reference Compensating Current Estimation Techniques for Shunt Active Filter**

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#### Abstract:

A shunt active filter injects a suitable non-sinusoidal current (compensating current) into the system at the point of common coupling and makes the source current sinusoidal. This paper presents a performance comparison of five different methods of estimating reference-compensating current for a three-phase shunt active power filter. The techniques compared are Instantaneous Active and Reactive power p-q method, Instantaneous Power Balance method, Instantaneous Active and Reactive current component id-iq method, Fourier series method and DC-link voltage regulation method. Their performance is investigated under ideal (balanced and sinusoidal), non-ideal (un-balanced and distorted) supply voltage conditions and at different load conditions. A three-phase six-pulse converter with R-L load is considered as the non-linear load. The MatLab/simulink simulation results are presented to validate and compare the control techniques in transient and steady state conditions.

*Key words:* Power quality, Active power filter, Comparative analysis, Harmonic and Reactive power compensation

### **1** Introduction

The proliferation of power electronic converters has led to the degradation of the power quality. The performance of SAPF depends on the method of extraction of the reference compensating current. This reference current and the actual SAPF current is given to a hysteresis based, carrier-less PWM current controller to generate the switching signals of the inverter.

Figure 1 shows the SAPF, which is controlled to supply a compensating current  $i_c$ at the point of common coupling (PCC) and cancels current harmonics on the supply side. Now, the source current  $i_s$  will be sinusoidal and in-phase with the supply voltage  $V_s$ . The organization of this paper is as follows. The different methods of estimating referencecompensating current are discussed and their performance is compared under ideal and nonideal mains voltage at different load conditions.



Fig. 1 Basic compensation principle of SAPF

### 2 Instantaneous active and reactive power p-q method [1]

Most active filters are designed based on the instantaneous active and reactive power pq theory. The active filter reference currents  $(\dot{i_{ca}}^{*}, \dot{i_{cb}}^{*}, \dot{i_{cc}}^{*})$  are obtained from the instantaneous active and reactive powers p<sub>L</sub> and q<sub>L</sub> of the non-linear load. This is achieved by transforming the mains voltage and load current into two-axis  $\alpha$ - $\beta$  co-ordinates by (1) and (2).

$$\begin{bmatrix} \mathbf{v}_{\alpha} \\ \mathbf{v}_{\beta} \end{bmatrix} = \sqrt{2/3} \cdot \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3/2} & -\sqrt{3/2} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{v}_{1} \\ \mathbf{v}_{2} \\ \mathbf{v}_{3} \end{bmatrix}$$
(1)

$$\begin{bmatrix} \mathbf{i}_{\mathbf{L}\alpha} \\ \mathbf{i}_{\mathbf{L}\beta} \end{bmatrix} = \sqrt{2/3} \cdot \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & \sqrt{3}/2 \end{bmatrix} \cdot \begin{bmatrix} \mathbf{i}_{\mathbf{L}a} \\ \mathbf{i}_{\mathbf{L}b} \\ \mathbf{i}_{\mathbf{L}c} \end{bmatrix}$$
...(2)

The instantaneous active and reactive powers  $p_L$  and  $q_L$  are expressed as

$$\begin{bmatrix} p_{L} \\ q_{L} \end{bmatrix} = \begin{bmatrix} v_{\alpha} & v_{\beta} \\ v_{\beta} & -v_{\alpha} \end{bmatrix} \cdot \begin{bmatrix} i_{L\alpha} \\ i_{L\beta} \end{bmatrix} \qquad \dots (3)$$

The instantaneous active and reactive powers can be decomposed into oscillatory and average terms as  $p_L = p_L = \widetilde{p}_L + P_L$  and  $q_L = \tilde{q}_L + Q_L$ . Under balanced and sinusoidal mains voltage conditions, the average power components are related to the fundamental current and the oscillatory components represent all higher order current harmonics. After eliminating the average power components by low-pass filter (LPF), the powers to be compensated are  $p_c = -\widetilde{p}_L$  and  $q_c = - \tilde{q}_L$ . The reference compensation currents are obtained by inverting the matrix in (3). These currents can be calculated by (4) and (5).

$$\begin{bmatrix} \mathbf{i}_{c\alpha} \\ \mathbf{i}_{c\beta} \end{bmatrix} = \frac{1}{\mathbf{v}_{\alpha}^{2} + \mathbf{v}_{\beta}^{2}} \cdot \begin{bmatrix} \mathbf{v}_{\alpha} & \mathbf{v}_{\beta} \\ \mathbf{v}_{\beta} & -\mathbf{v}_{\alpha} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{p}_{c} \\ \mathbf{q}_{c} \end{bmatrix} \dots (4)$$

$$\begin{bmatrix} \mathbf{i}_{ca}^{*} \\ \mathbf{i}_{cb}^{*} \\ \mathbf{i}_{cc}^{*} \end{bmatrix} = \sqrt{2/3} \cdot \begin{bmatrix} 1 & 0 \\ -1/2 & \sqrt{3/2} \\ -1/2 & -\sqrt{3/2} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{i}_{ca} \\ \mathbf{i}_{c\beta} \end{bmatrix}$$
...(5)



Fig. 2 Generation of reference compensating current by p-q method

### **3** Instantaneous power balance method [4]

The conventional instantaneous active and reactive power p-q theory needs coordinate transformations (a-b-c to  $\alpha$ - $\beta$  and vice versa). In this method, the compensating current is determined based on the balance of the instantaneous active and reactive power generated in the SAPF. The three phase instantaneous active power consumed by the load is

$$p_L = v_a i_{La} + v_b i_{Lb}(t) + v_c i_{Lc}$$
 ...(6)

The three phase instantaneous reactive power in each phase becomes

$$\begin{array}{l} q_{La} = v_{b} \ i_{Lc} - v_{c} \ i_{Lb} \\ q_{La} = v_{c} \ i_{La} - v_{a} \ i_{Lc} \\ q_{La} = v_{a} \ i_{Lb} \ - v_{b} \ i_{La} \end{array} \qquad ...(7)$$

The instantaneous active and reactive power delivered to a nonlinear load must satisfy (8) and (9).

$$p_L = p_s + p_c = p_{L1} + p_{Lh} \qquad ...(8) q_{fk} = q_{Lk}, k = a,b,c \qquad ...(9)$$

$$q_{fk} = q_{Lk}, k = a, b, c$$

where  $p_s$  - instantaneous active power

supplied by the source

p<sub>f</sub> -instantaneous active power supplied by the SAPF

p<sub>L1</sub> - instantaneous active fundamental power of the load

p<sub>Lh</sub> - instantaneous harmonic power of the load q<sub>Lk</sub> - instantaneous reactive power generated

by the SAPF at phase k.

In order to ensure that the fundamental active power is supplied to the load from the source, the instantaneous reactive power and harmonic power must be compensated by the SAPF. When considering the compensation of both harmonic and reactive power, p<sub>f</sub> is expressed as

$$p_c = v_a i_{ca} + v_b i_{cb} + v_c i_{cc} = p_{Lh}$$
 ...(10)

From (9) and (10), the reference compensating currents are determined as:

$$i_{ck} = i_{Lk} - \frac{p_{Ll}}{v_a^2 + v_b^2 + v_c^2} v_k$$
, k = a, b,c ...(11)



Fig. 3 Generation of reference compensating current by power balance method

# 4 Instantaneous active and reactive current component $i_d$ - $i_q$ method [3]

In this method, the reference compensating currents  $i_c^*$  are obtained from the instantaneous active and reactive current components  $i_{Ld}$  and  $i_{Lq}$  of the non-linear loads. The supply voltages and the load current in a-b-c coordinates are transformed to into two-axis  $\alpha$ - $\beta$  co-ordinates by (12) and (13). The dq load current components are derived from a synchronous reference frame based on the Park transformation, where  $\theta$  represents the instantaneous voltage vector angle.

$$\begin{bmatrix} \mathbf{i}_{\mathrm{Ld}} \\ \mathbf{i}_{\mathrm{Lq}} \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix} \cdot \begin{bmatrix} \mathbf{i}_{\mathrm{L\alpha}} \\ \mathbf{i}_{\mathrm{L\beta}} \end{bmatrix} \qquad \dots (12)$$

$$\theta = \tan^{-1}(v_{\alpha}/v_{\beta}) \qquad \dots (13)$$

Under balanced and sinusoidal supply voltage conditions, angle  $\theta$  is a uniformly increasing function of time. This transformation angle is sensitive to voltage harmonics and unbalance. Using (12) in (13) we obtain

$$\begin{bmatrix} i_{Ld} \\ i_{Lq} \end{bmatrix} = \frac{1}{\sqrt{v_{\alpha}^{2} + v_{\beta}^{2}}} \cdot \begin{bmatrix} v_{\alpha} & v_{\beta} \\ -v_{\beta} & v_{\alpha} \end{bmatrix} \cdot \begin{bmatrix} i_{L\alpha} \\ i_{L\beta} \end{bmatrix} (14)$$



### Fig. 4 Generation of reference-compensating current by i<sub>d</sub>-i<sub>g</sub> method

The instantaneous active and reactive components of the load currents can be decomposed into oscillatory and average terms as:  $i_{Ld} = \tilde{i}_{Ld} + I_{Ld}$  and  $I_{Lq} = \tilde{i}_{Lq} + I_{Lq}$ . The fundamental current, which constitutes the average current component, is eliminated from the all-higher order harmonic component (oscillatory component) using a low-pass filter. The currents to be compensated are  $i_{cd} = -\tilde{i}_{cd}$  and  $i_{cq} = \tilde{i}_{cq}$ . The compensation currents in two-axis  $\alpha$ - $\beta$  co-ordinates is obtained from (15).

$$\begin{bmatrix} \mathbf{i}_{c\alpha} \\ \mathbf{i}_{c\beta} \end{bmatrix} = \frac{1}{\sqrt{\mathbf{v}_{\alpha}^{2} + \mathbf{v}_{\beta}^{2}}} \cdot \begin{bmatrix} \mathbf{v}_{\alpha} & -\mathbf{v}_{\beta} \\ \mathbf{v}_{\beta} & \mathbf{v}_{\alpha} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{i}_{cd} \\ \mathbf{i}_{cq} \end{bmatrix} (15)$$

The reference compensation currents in ab-c co-ordinates are obtained from (16).

$$\begin{bmatrix} \mathbf{i}_{ca}^{*} \\ \mathbf{i}_{cb}^{*} \\ \mathbf{i}_{cc}^{*} \end{bmatrix} = \sqrt{2/3} \cdot \begin{bmatrix} 1 & 0 \\ -1/2 & \sqrt{3/2} \\ -1/2 & -\sqrt{3/2} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{i}_{c\alpha} \\ \mathbf{i}_{c\beta} \end{bmatrix}$$
...(16)

### **5** Fourier series method [5]

In this method, the referencecompensating current is obtained from the fundamental component of the load current. According to Fourier series, the instantaneous periodical load current  $i_L(t)$  can be expressed as

$$\dot{\mathbf{u}}_{L}(t) = \sum_{n=1}^{N} \sqrt{2} \mathbf{I}_{Ln} \sin(n\omega t + \phi_n)$$

$$= \sqrt{2} I_{L1} \cos\phi_1 . \sin(\omega t) + \sqrt{2} I_{L1}$$
  

$$\sin\phi_1 . \cos(\omega t) + \sum_{n=2}^{N} \sqrt{2} I_{Ln} \sin(n\omega t + \phi_n) \qquad \dots (17)$$

where

$$\begin{split} &\omega = 2\pi f - \text{fundamental angular frequency} \\ &I_{Ln} \text{ - rms value of the nth harmonic current} \\ &\varphi_n \text{ - phase angle of the nth harmonic current} \\ &The load current has three components namely \\ &i_L(t) = i_{Lp}(t) + i_{Lq}(t) + i_{Lh}(t) \qquad \dots (18) \\ &\text{where } i_{Lp}(t) = \sqrt{2} I_{L1} \cos(\phi_1).\sin(\omega t) \text{ - active} \\ &\text{fundamental component} \qquad \dots (19) \end{split}$$

$$i_{Lq}(t) = \sqrt{2} I_{L1} \sin(\phi_1) . \cos(\omega t) -$$

reactive fundamental component

$$\dot{a}_{Lh}(t) = \sum_{n=2}^{N} \sqrt{2} I_{Ln} \sin(n\omega t + \phi_n) -$$

harmonic component

Multiplying (17) with sinot and integrating between zero and T gives

$$\int_{0}^{T} i_{L}(t) . \sin(\omega t) . dt = \int_{0}^{T} \sqrt{2} I_{L1} . \cos(\phi_{1}) . \sin^{2}(\omega t) dt$$
$$= T/2. \sqrt{2} I_{L1} \cos(\phi_{1}) \dots ... (20)$$

Substituting (20) into (19), the active fundamental component of load current becomes

$$i_{Lp}(t) = \left[\frac{2}{T}\int_{0}^{T} i_{L}(t).\sin(\omega t) dt\right] \sin(\omega t) \qquad \dots (21)$$

The reference current of active power filter can be easily obtained by subtracting the load current from its active fundamental component.

$$i_c^{*}(t) = i_L(t) - i_{Lp}(t)$$
 ...(22)



Fig. 5 Generation of reference source current by Fourier series method

## 6 DC link voltage regulation method [2, 6]

In this method, peak value of the reference source current is obtained by

regulating the dc side capacitor voltage of the PWM inverter. This capacitor voltage is compared with a reference value and the error is processed in a PI controller. The reference source current is obtained by multiplying this peak value with the unit sine vectors that are in-phase with the supply voltage.

If non-linear load is applied, then the load current will have fundamental, reactive and harmonic components, which can be represented as

$$\begin{split} \dot{\mathbf{u}}_{L}(t) &= \sum_{n=1}^{\infty} \mathbf{I}_{Ln} \ .sin(n\omega t + \phi_n) \qquad \dots (23) \\ &= \mathbf{I}_{L1}.sin(\omega t + \phi_1) + \sum_{n=2}^{\infty} \mathbf{I}_{Ln} \ .sin(n\omega t + \phi_n) \end{split}$$

The instantaneous load power can be given as  $p_L(t) = v_s(t) . i_L(t)$ 

$$= V_{m} I_{L1} \cos(\phi_{1}) \cdot \sin^{2}(\omega t) + V_{m} I_{L1} \sin(\phi_{1}) \cdot \sin(\omega t) \cdot \cos(\omega t) + V_{m} \sin(\omega t) \cdot \sum_{n=2}^{\infty} I_{Ln} \sin(n\omega t + \phi_{n})$$

 $= p_{f}(t) + p_{r}(t) + p_{h}(t) \qquad \dots (24)$ From (24), real power drawn by the load  $p_{f}(t) = V_{m}I_{L1}\cos(\phi_{1}).Sin^{2}(\omega t) = v_{s}(t).i_{s}(t)...(25)$ From (25), source supplied by the source after compensation is

$$\begin{split} i_s(t) &= p_f(t) / \ v_s(t) = I_{L1} \cos(\varphi_1) \ . \ Sin \ (\omega t) \\ &= I_{sm} sin \ (\omega t) \end{split}$$

where,  $I_{sm} = I_{L1} \cos(\phi_1)$  ...(26)

The utility has to supply for the capacitor leakage and inverter switching losses in addition to the real power of the load. Hence, total peak current supplied by the source is expressed as

$$I_{sp} = I_{sm} + I_{sL} \qquad \dots (27)$$

The reference source current is given by

$$i_s(t) = I_{sp.} \sin(\omega t)$$
 ...(28)

This peak value of the reference source current has been estimated by regulating the dc side capacitor voltage of the PWM inverter. The reference compensating current is obtained as

$$i_c^{*}(t) = i_L(t) - i_s^{*}(t)$$
 ...(29)



Fig.6 Generation of reference source current by DC link voltage regulation method

### 7 ComparativeAnalysis

The performance of different methods is investigated based on %THD of the source current after compensation under ideal (balanced and sinusoidal), non-ideal (unbalanced and distorted) supply voltage conditions and at different load conditions.

### 7.1 Ideal mains voltage

The balanced and sinusoidal threephase mains voltages considered for simulation are

From Fig. 7, it is observed that for all the five methods, THD of the source current is reduced well below 5% and meets IEEE-519 standards for the firing angle  $\alpha = 0^{\circ}$  and  $30^{\circ}$ . When  $\alpha = 60^{\circ}$ , THD exceeds the limits for pq theory,  $i_d$ - $i_q$  method and power balance method.



Fig.7 Comparative plots for five methods under balanced mains voltage and at different load conditions

### 7.2 Unbalanced mains voltage

The three-phase unbalanced and sinusoidal mains voltage considered for simulation is

 $v_a = 180 \sin(\omega t + 20^\circ)$ 

 $v_b = 200 \sin(\omega t - 120^{\circ})$ 

 $v_c = 230 \sin(\omega t + 120^\circ)$  ...(31)

Under unbalanced mains voltage, THD of the source current is reduced well below 5% for Fourier series method and DC link Voltage regulation method (Table 1). The performance of pq theory, power balance method and  $i_{d}$ - $i_{q}$  method deteriorates.

The unbalanced three-phase mains voltage can be decomposed into positive and negative sequence components. Even in the two-axis co-ordinates, the mains voltages contain positive and negative sequence components. Hence, the sum of  $v_{\alpha}^2$  and  $v_{\beta}^2$  will not be a constant. A second order and third order harmonic is observed in the compensated source current, where its amplitude depends on the negative sequence components. This leads to the degradation of the performance of pq method and  $i_d$ - $i_q$  method.

Fig.8 shows unbalanced mains voltage ( $v_{abc}$ ), load current ( $i_{Labc}$ ), source current ( $i_{Sabc}$ ) for pq method, Instantaneous Power Balance method, Instantaneous Active and Reactive current component  $i_d$ - $i_q$  method, Fourier series method and DC link Voltage regulation method respectively. It is observed that the source current is sinusoidal and balanced for Fourier series and DC link Voltage regulation method.

### 7.3 Distorted mains voltage

The following distorted three-phase mains voltage is considered for the simulation.  $v_a = 230 \sin(\omega t) + 25 \sin(5\omega t)$ 

 $v_b = 230 \sin(\omega t - 120^\circ) + 25 \sin(5\omega t - 120^\circ)$ 

 $v_c = 230 \sin(\omega t + 120^\circ) + 25\sin(5\omega t + 120^\circ)...(32)$ 

Under distorted mains voltage, the performance of pq theory, power balance method and  $i_d$ - $i_q$  method deteriorates. When the three-phase mains voltage is distorted, it can be decomposed as fundamental and harmonic components. The mains voltages in



Fig.8 Unbalanced mains voltage, Load current and Source current for different methods

the two-axis system contain the fundamental and harmonic components. As the sum of  $v_{\alpha}^{2}$  and  $v_{\beta}^{2}$  will not be a constant,  $(k-1)^{th}$  and/or  $(k+1)^{th}$  order harmonic is observed in the compensated source current. This factor leads to the degradation of performance of p-q, power balance method and id-iq method.





From (22) and (29), it is observed that the reference compensating current is independent of the mains voltage for Fourier series method and DC link voltage regulation method respectively. Hence, these two methods provide a good performance by maintaining THD of the source current at a

Reference	% THD of source current			% THD of source			No. of Multiplior	No. of
compensating current	for different load			load conditions under				current
Tashriswas	unbalanced supply			distante d supply			/ summer	/ Voltogo
Techniques				distorted supply			circuits	voltage
	voltage			voltage				sensors
	α=0°	α=30°	α=60°	α=0°	α=30°	α=60°		
% THD in source	25.68	34.25	53.60	18.50	29.03	43.11		
current before								
compensation								
Instantaneous	9.24	10.46	14.04	6.49	6.54	9.91	11/19	3/3
p-q method								
Power balance	16.49	16.19	17.71	6.47	6.45	9.94	7/7	3/3
method								
Instantaneous	6.48	6.57	9.42	6.54	7.48	7.16	12/15	3/3
i <sub>d</sub> -i <sub>q</sub> method								
Fourier series method	1.82	1.06	3.04	0.68	1.20	3.92	4/3	3/0
DC link voltage	1.05	1.58	3.07	1.81	2.60	3.69	2/4	3/1
regulation method								

Table 1 Comparison of different methods

value less than 5%. As the design of PI controller is simple and easy, DC link voltage regulation method is best suited for the compensation of harmonic and reactive power. Fig.10 shows its load perturbation response. The steady is reached after a delay of one cycle.



Fig.10 Load perturbation response

### 8 Conclusion

The performance of different reference compensating current estimation techniques is compared and investigated under ideal (balanced and sinusoidal), non-ideal (unbalanced and distorted) supply voltage conditions and at different load conditions.

Fourier series method and DC link voltage regulation method provides a good performance even under non-ideal (unbalanced and distorted) mains voltage conditions.

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