## Analysis of Voltage to Frequency Converter with Phase Modulation Possibility

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*Abstract:* - Voltage to frequency converter (VFC) is an oscillator whose frequency is linearly proportional to control voltage. In this paper, the New Synchronous Voltage to Frequency Converter (NSVFC) or "sigma delta" ( $\Sigma$ - $\Delta$ ) voltage to frequency converter is described. This NSVFC works similarly as conventional SVFC but it has a better frequency spectral property then other SVFC and therefore it is possible to used in fractional phase locked loop (PLL). More over, the NSVFC has a phase modulation possibility. A experimental NSVFC was constructed and simulated to verify operation of the converter. Analysis and prototype of NSVFC is described.

*Key-Words:* Voltage to frequency converter, fractional phase locked loop, sigma delta converter, frequency spectrum, phase modulation, frequency synthesizer.

## **1** Introduction

The VFC have become quite popular due to their low cost and application versatility in variety of electronic control and measurement systems. With a good quality VFC, this circuit will match the performance of many commercial A/D converters. Its only disadvantage is relatively slow conversion time.  $\Sigma$ - $\Delta$  modulator [1] can be used for synchronous VFC (SVFC). In SVFC charge balance pulse length is now defined by two successive edges of the external clock. The block diagram of the  $\Sigma$ - $\Delta$  VFC is shown on Fig. 1. If this clock has low jitter the charge will be defined very accurately. The output pulse will also be synchronous with the clock. SVFCs of this type are capable of up to 18-bit linearity and they have excellent temperature stability [2], but is not pure tone for constant input voltage (output pulses are not equally spaced). Fig. 2 c) shows the waveforms of  $\Sigma$ - $\Delta$  SVFC. From Fig. 2 c) can be seen that output periods are not the same, but they have changed between 3 and 4 clock cycles. This disadvantage was taken away in NSVFC1 and NSVFC2.

## 2 Description of new synchronous VFC

In Fig. 3 is NSVFC1 block diagram. Only one-shot is added and connected to comparator output. Fig. 2 shows waveforms of this NSVFC1. Number of pulses is same for usual  $\Sigma$ - $\Delta$  SVFC [2] and NSVFC (NSVFC1 and NSVFC2). The output frequency  $f_o$  is given by (1):

 $f_O = f_{CLK} (l - V_i / V_R) / 2$  [Hz, V] (1)

where  $V_i$  is input voltage,  $V_R$  is reference voltage and  $f_{CLK}$  is clock frequency. It is important to note, that for

NSVFC1 this equation is limited for  $V_{imin}$  given by (2). The minimal input voltage value  $V_{imin}$  (for NSVFC1):

 $V_{imin} > 2f_{CLK} V_R t_{dC}$  [V, Hz, sec] (2) where  $t_{dC}$  is comparator time delay. E.g. for  $f_{CLK} = 10$ kHz,  $V_R = 5 V$  and  $t_{dC} = 200$  ns, the minimal value  $V_{imin}$ > 0.02 V.



Figure 1. Conventional  $\Sigma$ - $\Delta$  voltage to frequency converter (SVFC). Int. - integrator, Comp. - comparator,  $V_i$  - input voltage,  $V_R$  - reference voltage, D - flip flop.



Figure 2. Waveforms of SVFC (a, c) and NSVFC (a, b, c). a) integrator - output voltage, b) one shot output, c) D-flip flop output.  $V_i = 1.8$  V,  $V_R = 4$  V, period of one shot is 3.636  $T_{clk}$ 

#### **3** V/f - output frequency evaluation

The key to  $\Sigma$ - $\Delta$  modulator is the integrator. At each conversion, the integrator keeps a running total of its previous output and its current input. The output from the integrator is feed to 1-bit analog/digital converter (ADC). This is simply a comparator with its reference input at a level of half the input range, 0 V in this case. The ADC output feeds a 1-bit digital/analog converter (DAC) which has output levels equal  $+V_R$  or  $-V_R$ . A summing amplifier completes the loop by summing the current input signal and the previous sample DAC output. The aim of the feedback loop is to try to maintain the average output change of the integrator at the comparator reference level, 0 V. Therefore:

$$const + \sum_{k=1}^{\infty} V_{o1}(k) + \sum_{k=1}^{\infty} V_{o2}(k) = 0$$
(3)

where k = 1, 2,..., $\infty$ , const is voltage depending on starting conditions and  $V_{o1}(k)$  and  $V_{o2}(k)$  are integrator output voltage in k output frequency period, see Fig. 4. The NSVFC and equivalent period time diagram is shown on Fig. 5.



Figure 3. NSVFC1 - New  $\Sigma$ - $\Delta$  voltage to frequency converter type1. Int. - integrator, Comp. - comparator,  $V_i$  - input voltage,  $V_R$  - reference voltage, D - flip flop, OS - one shot.



Figure 4. Time diagram for ideal converter - output frequency evaluation

Change  $\Delta V_a$  is given by (4):

$$\Delta V_a = C \int_{0}^{T_{clk}} (V_i(t) + V_R) dt$$
(4)

and  $\Delta V_b$  is given by (5):

V

$$\Delta V_b = C \int_0^{nT_{ck}} (V_i(t) - V_R) dt$$
<sup>(5)</sup>

where C is the integrator constant. The integrator output is given by:

$$V_{o2}(k) = V_{o1}(k) + C \int_{T_{clk}}^{(n+1)T_{clk}} (V_i(t) - V_R) dt$$
(6)

$$V_{o1}(k) = V_{o2}(k-1) + C \int_{0}^{T_{clk}} (V_i(t) + V_R) dt$$
(7)

and for  $V_i(t) = V_i$  (constant input voltage):

$$V_{ol}(k) = V_{o2}(k-1) + C(V_i + V_R)T_{clk}$$
(8)

$$V_{o2}(k) = V_{o1}(k) + C(V_i - V_R)nT_{clk}$$
 (9)

Integrator output voltage change is given by:

$$C(V_i + V_R)T_{clk} = C(V_i - V_R)nT_{clk}$$
(10)

where n must be an integer for SVFC. For NSVFC output is given by:

$$C(V_i + V_R)T_{clk} = C(V_i - V_R)mT_{clk}$$
(11)

where *m* is real for NSVFC. From (11)  $(V_R > V_i)$ :

$$n = \frac{V_i + V_R}{V_R - V_i} \tag{12}$$

and for SVFC, *n* is given by (13):

$$n = ceil\left(\frac{V_i + V_R}{V_R - V_i}\right) = ceil(m)$$
(13)

where Ceil(.) - Converts a numeric value to an integer by returning the smallest integer greater than or equal to its argument. E.g. Ceil(9/3)=3, Ceil(9.01/3)=4.

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# 4 Output frequency evaluation for ideal V/f converter

For this ideal NSVFC it is supposed, that comparator has a zero time delay and noise value voltage on second comparator input is zero. Output period for NSVFC can be determined from Fig. 4. It is supposed, that  $V_R > V_i$ , where  $V_R$  is reference voltage and  $V_i$  is input voltage. The  $V_L(i)$  and  $V_H(i)$  are voltage at integrator output.

Output period  $T_0$  from Fig. 6 is given by:

$$T_0 = T_{clk} \left[ n(k+1) - t_z(k+1) + 1 + t_z(k+2) \right]$$
(14)

Time from  $V_L(i)$  to  $V_H(i+1)$  is always  $l^*T_{clk}$  if no error occurs (error can be caused by comparator delay, comparator hysteresis or voltage change on second comparator input. This will discuss in next part). For  $T_{clk}$ = 1, the output period  ${}^{I}T_{0}$ :

$${}^{I}T_{0} = n(k+1) - t_{z}(k+1) + 1 + t_{z}(k+2)$$
(15)

Strait line from  $V_L(i)$  to  $V_H(i+1)$  has a slope:  $V_i + V_R$ The line is given by equation (all following equations are given for  $T_{clk} = I$ ):

$$V_{H}(k+1) = V_{L}(k) + (V_{i} + V_{R}).1$$
(16)

The line slope from  $V_H(i)$  to  $V_L(i+1)$  is:  $V_R - V_i$ . Line equation is:

$$V_L(k+1) = V_H(k+1) - (V_R - V_i) n(k+1)$$
(17)

where n(k+1) is given by: 7) 1/17 /1

$$n(k+1) = ceil(V_H(k+1)/(V_R - V_i)) = ceil((V_L(k) + V_R + V_i)/(V_R - V_i))$$
(18)

hence

$$V_{L}(k+1) = V_{H}(k+1) - (V_{R} - V_{i}) n(k+1) =$$

$$V_{H}(k+1) - (V_{R} - V_{i}) ceil(V_{H}(k+1)/(V_{R} - V_{i})) = (19)$$

$$V_{L}(k) + V_{i} + V_{R} - (V_{R} - V_{i}) ceil((V_{L}(k) + V_{R} + V_{i})/(V_{R} - V_{i}))$$

The term  $(V_R - V_i)$  ceil $((V_L(k) + V_R + V_i)/(V_R - V_i))$ can't be reduced, because ceil() is nonlinear function, e.g.:  $y(ceil(x/y)) \neq ceil(x)$ .

Time  $t_z(k)$  is given by:

$$t_z(k) = V_H(k)/(V_R - V_i)$$
 (20)

Output period equation is given by (for  $T_{clk} = I$ ):

$${}^{T}T_{0} = n(k+1) - t_{z}(k+1) + 1 + t_{z}(k+2) =$$

$$ceil((V_{L}(k) + V_{R} + V_{i})/(V_{R} - V_{i})) - V_{H}(k+1)/(V_{R} - V_{i})$$

$$+ 1 + V_{H}(k+2)/(V_{R} - V_{i})$$
(21)

After multiplication by term  $(V_R - V_i)$ , equation (21) is changed to:

$$(V_R - V_i)^{T} T_0 = (V_R - V_i) \ ceil((V_L(k) + V_R + V_i)/(V_R - V_i))$$
  
-  $(V_L(k) + V_R + V_i) + V_R - V_i + V_L(k+1) + V_R + V_i$  (22)  
 $V_i(k+1)$  is substitute by equation (10) hence:

 $V_L(k+1)$  is substitute by equation (19), hence:

$$(V_R - V_i)^{T} T_0 = (V_R - V_i) ceil((V_L(k) + V_R + V_i)/(V_R - V_i)) - (V_L(k) + V_R + V_i) + 2V_R + V_L(k) + V_i + V_R - (V_R - V_i) ceil((V_L(k) + V_R + V_i)/(V_R - V_i))$$
(23)

$$cell((V_L(k) + V_R + V_i)/(V_R - V_i))$$
(22)

After reduction, output period  ${}^{T}T_{\theta}$  is given by:

$${}^{T}T_{0} = 2V_{R} / (V_{R} - V_{i})$$
 (24)

and output frequency  ${}^{l}f_{0}$  hence:

$${}^{I}f_{0} = (V_{R} - V_{i})/2V_{R}$$
(25)

and for  $T_{clk} \neq l$  the output frequency  $f_0$ :  $f_0 = f_{clk} (V_R - V_i)/2V_R$ (26)

where  $f_{clk} = 1/T_{clk}$ 

From (26) is shown, that ideal NSVFC output frequency is linearly dependent on input voltage ( $f_{clk}$  and  $V_R$  are constants).

## **5** Output Frequency Evaluation for Real V/f converter

In this part, error caused by comparator delay, comparator hysteresis or voltage change on second comparator input is described. This error is displayed on Fig. 5 and is sign by X point. The error can arise especially when input voltage  $V_i \approx 0$ . The error occur when 2 clock cycles are need for  $V_L(k)$  to  $V_H(k+1)$ transition. In this case, this must be detected and additional output pulse is generated, when integrator output voltage on one comparator input is greater than voltage on second comparator input (it is important to note, that in ideal condition, output pulse is generated only when voltage on integrator output is lower then voltage on second comparator input - leading edge of integrator output). The additional logic is used for this purpose. The block diagram of this NSVFC2 is shown in Fig. 6.

Output period  $T_0$  from Fig. 5 is given by:

$$T_{el} = T_{clk} [n(k) - t_{z}(k) + t_{e}(k)]$$
(27)  
For  $T_{clk} = l$ ,  $V_{i} << V_{R}$  output period  ${}^{l}T_{el}$  is given by:  
 ${}^{l}T_{el} = ceil(V_{H}(k)/(V_{R} - V_{i})) - V_{H}(k)/(V_{R} - V_{i})$   
 $+ |V_{L}(k)/(V_{R} + V_{i})|$ (28)

In (28)  $ceil(V_H(k)/(V_R - V_i))=2$  and  $V_H(k) \approx V_R$  and  $|V_L(k)| \approx V_R$  for  $V_i \approx 0$ . Hence:

 ${}^{l}T_{el} = 2 - V_{R} / (V_{R} - V_{i}) + V_{R} / (V_{R} + V_{i}) \approx 2(1 - V_{i} / V_{R})$ (29) Similarly the output period  ${}^{1}T_{e2}$  is given by:

$${}^{l}T_{e2} = 2 - t_{e}(k) + V_{R}/(V_{R} - V_{i})$$
  
=2-V<sub>R</sub>/(V<sub>R</sub> + V<sub>i</sub>)+V<sub>R</sub>/(V<sub>R</sub> + V<sub>i</sub>) ≈ 2(1+V<sub>i</sub>/V<sub>R</sub>) (30)

Equations (29) and (30) for  $T_{clk}$  are simplified to:

$$T_{el} \approx 2T_{clk} \left( 1 - V_i / V_R \right) \tag{31}$$

$$T_{e2} \approx 2T_{clk} \left( 1 + V_i / V_R \right) \tag{32}$$



Figure 5. Time diagram for real converter - output frequency evaluation.  $T_{e1}$  and  $T_{e2}$  are output frequency periods, Px is generated by correction logic.

#### 6 Phase Modulation

The NSVFC2 has phase modulation capabilities. When the modulating voltage  $V_{PM}$  is applied to second comparator input, see Fig. 6, the output signal is phase modulated. The  $V_{PM} < V_R$  must be satisfied for modulation voltage. The time diagram for phase modulation computing is shown on Fig. 7.

For  $T_{clk} = I$ , the output period  ${}^{I}T_{PM}$  is given by (33):

$$T_{PM} = n(k+1) - t_z(k+1) + 1 + t_{zPM}(k+2)$$
 (33)

The equation for n(k+1) and  $t_z(k+1)$  are the same as (18) and (20). But  $t_{zPM}(k+2)$  is:

 $t_{zPM}(k+2) = (V_H(k+2) - V_{PM})/(V_R - V_i)$ (34) where  $V_{PM}$  is voltage on second comparator input.

After some mathematics manipulation the  ${}^{T}T_{PM}$  is:

$${}^{T}T_{PM} = (2V_{R} - V_{PM})/(V_{R} - V_{i}) =$$

$$2V_{R}/(V_{R} - V_{i}) - V_{PM}/(V_{R} - V_{i}) = {}^{1}T_{o} - \Delta^{1}T_{PM}$$
(35)

hence  $\Delta \varphi$  is given by (36):

$$\Delta \varphi = \pi V_{PM} / V_R \text{ [rad, -]}$$
(36)

From (36) is shown, that NSVFC2 phase change is linearly dependent on input voltage  $V_{PM}$ .



Figure 6. NSVFC2 - Block diagram. Int. - integrator, C - comparator, V<sub>i</sub> - input voltage, V<sub>r</sub> - reference

voltage,  $V_{PM}$  - input voltage for phase modulation, D - flip flop, OS - one shot, AND, OR - log. function.



Figure 7. Time diagram for phase modulation evaluation



Figure 8. Experimental NSVFC1 simplified circuit diagram.



Figure 9. The frequency spectrum of traditional  $\Sigma$ - $\delta$  V/f converter



Figure 10. The frequency spectrum of new, modified  $\Sigma$ - $\delta$  V/f converter (NSVFC1).

#### 7 Experimental Results

Commercially produced SVFC AD7741 and AD7742 [2] were tested and also NSVFC1 was realized and tested [12], [13], [14], [15]. In Fig. 8, experimentally realized NSVFC1 simplified circuit diagram is shown [3]. The voltage/frequency characteristic and frequency spectrum was measured. In common type of SVFC, since the output pulses are synchronized to a clock they are not equally spaced. This need not affect the user of a SVFC for A/D conversion [16], [17], but it does prevent its use as a precision oscillator. Despite this disadvantage the improvement in performance makes the SVFC ideal for the majority of high-resolution VFC applications. In Fig. 9, the frequency spectrum of SVFC is shown and in Fig. 10, the spectrum of NSVFC1 is displayed. From Fig. 10 can be seen, that spurious spectral lines are rejected.



Figure 11. The block diagram of experimental fractional PLL synthesizer with  $\Sigma$ - $\delta$  V/f converter (NSVFC) used

as fractional divider,  $f_r$  - ref. frequency,  $f_o$  - output

frequency,  $V_i$  - control voltage, GEN - generator,

PD - phase detector, LPF-lowpass filter, VCO - voltage controlled oscillator.

 $\Sigma$ - $\delta$  V/f converter can be used for frequency synthesizer. The block diagram of experimental fractional PLL synthesizer is shown in Fig. 11. If the VCO is locked to the reference frequency, then:

$$f_d = f_r \tag{37}$$

where is  $f_r$  reference frequency and  $f_d$  is frequency on the output of NSVFC. Because is given by (38):

$$f_d = f_o (1 - V_i / V_R) / 2$$
(38)

where  $f_o$  is frequency of VCO. After substituting for  $f_d$  from (38) into equation (37), frequency of VCO is given by (39):

$$f_o = 2f_r \, l/(l - V_i/V_R) \tag{39}$$

The VCO frequency  $f_o$  can be changed according equation (39) by means of changing  $V_i$ .

#### 8 Conclusion

A very detailed look at the concept of new type sigmadelta voltage to frequency converter circuit has been presented in this article. A prototype system was constructed to verify operation of the converter, also analysis of new type voltage to frequency converter was described. The NSVFC simulation results and measured results were compared. From analysis, simulation and measured results can be seen very good agreement from different point of view. It was pointed out that this new converter has better properties than other synchronous types of VFC. This main disadvantage of SVF described above was removed in new type of NSVFC. Because output pulses are equally spaced in NSVFC (some spurious spectral lines are rejected), this device can be used also as fractional frequency divider.

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## Appendix

NSVFC2 block diagram for simulation in MATLAB is shown in Fig. A1. D Flip-Flops with Delays are used as one-shot blocks. The constant input voltage  $V_i = 0.15$  V is used, sinusoidal voltage (Phase mod. block) is used for phase modulation input in Fig. A1.



Figure A1. NSVFC2 block diagram for simulation in MATLAB