# Design of Multi Agent Adaptive Neuro-Fuzzy Based Intelligent Controllers for Multi-Objective Nonlinear System

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*Abstract:* - In this paper, we describe a multi agent controller for meeting different criteria, based on emotional learning. Our proposed controller is motivated by the affective and emotional faculties in human begins, which constantly evaluate the current states with respect to the achievement of the desired goals. For meeting different criteria, the controller consists of several critic agents that each agent tries to meet its goal. The combination of emotions of these agents applies on the controller in order to adapt the learning coefficients to achieve predefined criteria and goals. Our proposed controller, also continuously evaluate the current states from critic agents and incremental achievement or disachievement of the set objectives, and self tune its control action accordingly. The controller is based on intelligent neurofuzzy architecture that suitable for online training algorithms. The effectiveness of the total multi agent emotional control system (MEAC) is demonstrated trough examples in which the proposed system is used for reducing control effort and tracking error simultaneously. The contribution of critic's emotions in multi criteria satisfaction is highlighted through these examples.

Key-Words: - Multi-agent systems, Multiobjective, Neural Network, Fuzzy logic, Nonlinear systems

# **1** Introduction

In recent years, there have been many researches in multi agent controllers [1], [2]. In multi agent controllers, there are more than one controller or optimization/adaptation criteria that we called them agent and each agent is trying to reach to its goal independently. Each agent analyzes the control results with predefined criteria and produces an emotional feedback. These emotional feedbacks are used to make necessary changes in learning coefficients of controller in order to satisfy critic agent goals. Emotional Learning is one of powerful learning methods that its dates back to the early research work in psychology, neuro science and computer science. Emotional learning can be categorized in reinforcement learning methods [3]. In the last twenty years, there have been rapidly increasing interest in reinforcement learning and mainly in emotional learning. Emotional learning is a kind of unsupervised learning methods for autonomous agents to acquire action rules to adapt clue of emotional reward and punishment. In emotional learning the teacher of conventional supervised learning is replaced by an intelligent critic that assesses the performance of controller and evaluates the current states of system and generates proper emotional reinforcement signal [4]. Fuzzy system theory provides a mathematical framework for modeling vagueness and imprecision data [5]. Neural networks have the ability to learn complex mapping, generalize known data and classify inputs [6]. Hybrid system utilizes the advantages of both, as well as other novel techniques, creating powerful tools for intelligent control [7]. In this paper we use a powerful architecture for the main controller [8] and use multi agent critics in order to train the main controller so that can satisfy all critics' criteria and emotions. By using of emotional learning, our proposed multi agent controller can be learned to satisfy all critics simultaneously. On line training, fast convergence of controller and robustness of proposed controller are other advantages of this method that be shown by some simulation results.

## 2 Multi Agent Emotional Controller

In this section we describe proposed multi agent emotional controller. The block diagram of proposed system is shown in figure 1. As shown in this figure, it contains four main items as: controller, plant, emotional critic agents and learning mechanism. In the subsequent sections, we briefly discuss the above elements.

## A. Neurofuzzy Controller

Two major approaches of trainable neurofuzzy models can be distinguished. The network based

Takagi-Sugeno fuzzy inference system and the locally linear neurofuzzy model. It is easy to see that locally linear model is equivalent the to Takagi-Sugeno fuzzy model under certain conditions, and can be interpreted as an extension of normalized RBF network well. as The Takagi-Sugeno fuzzy inference system is based on fuzzy rules of the following type:

$$\begin{aligned} Rule_{i} : & If \ u_{1} = A_{i1} \ And \ \dots \ And \ u_{p} = A_{ip} \\ then \ y = f_{i} (u_{1}, u_{2}, ..., u_{p}) \end{aligned} \tag{1}$$



Fig 1 - Block diagram of Multi agent Neuro-Fuzzy Based Intelligent Controller

Where i = 1...M and M is the number of fuzzy rules.  $u_1,...,u_p$  are the inputs of network, each  $A_{ij}$  denotes the fuzzy set for input  $u_j$  in rule i and  $f_i(.)$  is a crisp function which is defined as a linear combination of inputs in most applications

$$y = \omega_{i0} + \omega_{i1}u_1 + \omega_{i2}u_2 + \dots + \omega_{ip}u_p$$
(2)

Thus the output of this model can be calculated by

$$y = \frac{\sum_{i=1}^{M} f_i(\underline{u})\mu_i(\underline{u})}{\sum_{i=1}^{M} \mu_i(\underline{u})} \qquad \mu_i(\underline{u}) = \prod_{j=1}^{p} \mu_{ij}(u_j) \qquad (3)$$

A simple form of  $f_i(u)$  can be as

$$f_i(u) = a_i u_1 + b_i u_2 + c_i$$
 (4)

The out put of controller is in the following form:

$$y = \frac{\sum_{i=1}^{n} \mu_i (a_i u_1 + b_i u_2 + c_i)}{\sum_{i=1}^{n} \mu_i}$$
(5)

Where *n* is number of controller fuzzy rules,  $\mu_i$  is the firing strength of i'th rules,  $u_i$  is the first and  $u_2$  is the second one for two input type controller (for example error and its derivative). In this paper we choose  $u_1 = e$  and  $u_2 = \dot{e}$ . The neurofuzzy controller applied in this paper, is a standard Sugeno fuzzy controller composed of four layers. In the first layer, all inputs are mapped into the range of [-1, +1]. In the second layer, the fuzzification process is performed using Gaussian membership functions with five labels for each input. In layer 3, decision-making is done using

Max-Product law and defuzzification is carried out in the fourth layer in order to calculate the proper control input using (5),  $a_i$ ,  $b_i$ ,  $c_i$  are parameters to be determined via learning mechanism.

## B. Critic

The most important blocks in figure 1 are the emotional critics. Emotional Critic is the main part of any emotional learning system. The performance of the critic can be compared with the performance of emotional hue in humans. In absence of an exact evaluation of the present state in term of the objective value function, emotional cues like stress, satisfaction and etc. can be guide our control action into changing in the right direction so as to produce desired response. Similarly, the critic evaluates the state of system and generates a signal called emotion (r). In multi agent system there are more than one critic that each of then evaluate the performance of system from their own point of view. For example in this paper we proposed a multi agent controller with two critics. One critic is satisfied by the low control error and another one is satisfied by low control cost and action. These emotion signals are used to train and fine tune the main controller. Basically these

> Po е NE ZF Ρo PS ZE Po PВ ZE NS ZE PS NE ZE NF NB NS PB = Positive Big PS = Positive Small NS = Negative Small NB = Negative Big ZE = Zero

Fig 2 - Rule base and fuzzy sets of first critic

#### C. Learning Mechanism

The main objective of learning mechanism is to satisfy total emotion and reduces total stress. This aim can be extracted trough bellow energy function:

$$E = \frac{1}{2} \qquad (k_1 r_1^2 + k_2 r_2^2) = E_1 + E_2 \tag{6}$$

By minimizing this energy function, we can reduce the total stress of the system and satisfy all critics. critics act as intelligent guides for the controller. The learning mechanism will be adapted the controller in order to satisfy all critics and reduce the stresses of them. Both of these critics are define in fuzzy forms. Fuzzy systems are very useful for critic modeling because the critic just gives us an approximate evaluation of current states of system. The first critic satisfies when the control error reach to zero. For this plan, the inputs of critic are error of plant output from desired response and its derivative. The emotion (output) of critic is a signal between [-1, 1] and shows the performance of the system. If this emotion becomes zero, it means that the critic is satisfied by the performance of controller. If the emotion becomes larger, it shows the more stress and more dissatisfaction. The fuzzy sets and rules base of this critic is shown in figure 2. The second critic will be satisfied by the low control cost. If control action becomes larger, it causes more stress in the critic output. The emotion of this critic is a signal between [0, 1] that 0 indicate better controller performance. The fuzzy sets and rules base of this critic is shown in figure 3.



Fig 3 - Rule base and fuzzy sets of second critic

With applying Newton gradient decent method the changes in weight must be followed by bellow general rule:

$$\Delta \mathbf{w}_{i} = \Delta \mathbf{w}_{i1} + \Delta \mathbf{w}_{i2} = -\eta \frac{\partial \mathbf{E}}{\partial \mathbf{w}_{i}}$$
$$= -\eta \left( \frac{\partial \mathbf{E}_{1}}{\partial \mathbf{w}_{i1}} + \partial \frac{\partial \mathbf{E}_{2}}{\partial \mathbf{w}_{i2}} \right)$$
(7)

Where  $\eta$  is the learning rate of the corresponding neurofuzzy controller. In order to calculate the RHS of (7), the chain rule is used:

$$\Delta \omega_{i1} = -\eta \frac{\partial E_1}{\partial r_1} \cdot \frac{\partial r_1}{\partial y} \cdot \frac{\partial y}{\partial u} \cdot \frac{\partial u}{\partial \omega_i}$$
(8)

From (6): 
$$\frac{\partial E}{\partial r_1} = k_1 r_1$$
 (9)

and also: 
$$e = y_{ref} - y$$
 (10)

then: 
$$\frac{\partial r_1}{\partial y} = -\frac{\partial r_1}{\partial e}$$
 (11)

Since with the incrimination of error,  $r_1$  will also be incremented and on the other hand, on-line calculation of  $\frac{\partial r_1}{\partial e}$  is accompanied with measurement errors, thus producing unreliable results, we have

$$\frac{\partial r_1}{\partial y} = -\frac{\partial r_1}{\partial e} = -\lambda \qquad (\lambda > 0) \tag{12}$$

that only the sign of it (-1) is used in our calculations. Also,  $\frac{\partial y}{\partial u} = J$ , where *J* is a Jacobian Matrix of the system. From (7) to (12),  $\Delta \omega_{i_1}$  will be calculated as follows:

$$\Delta \omega_{i1} = \eta k \ r_1 J \cdot \frac{\partial u}{\partial \omega_{i1}} \tag{13}$$

To follow up equation (6) to (13)  $\Delta \omega_{i2}$  can be calculated as:  $\Delta \omega_{i2} = \eta k_2 r_2 J \cdot \frac{\partial u}{\partial \omega_{i2}}$  (14)

From equation (6), (13) and (14)  $\Delta \omega_{i2}$  is calculated as:

$$\Delta \omega = \Delta \omega_1 + \Delta \omega_2 = \eta (K_1 r_1 + K_2 r_2) \cdot \frac{\partial u}{\partial \omega_i}$$
(15)

Equation (15) is used for updating the learning parameters  $a_i$ 's,  $b_i$ 's and  $c_i$ 's in (5), which is straightforward:

$$a_{i \text{ new}} = a_{i \text{ old}} + \eta (K_1 r_1 + K_2 r_2) \frac{e u_i}{\sum_{i=1}^n u_i}$$
$$b_{i \text{ new}} = b_{i \text{ old}} + \eta (K_1 r_1 + K_2 r_2) \frac{\dot{e} u_i}{\sum_{i=1}^n u_i}$$

$$c_{i \text{ new}} = c_{i \text{ old}} + \eta (K_1 r_1 + K_2 r_2) \frac{u_i}{\sum_{i=1}^n u_i}$$

In above formula,  $k_1$  and  $k_2$  are importance coefficient of emotions and indicate that with critic is more important and  $\eta$  is the learning coefficient that must be select proper value in order to both increase the learning speed and prevent the learning instability. It is recommended that this value is assumed between [0, 10].

# **3- Simulation Results**

The following simulation results illustrate the capabilities of proposed multi agent controller. In these simulations we choose a nonlinear model of HVAC system which it has delayed behavior and also is a multivariable, nonlinear non minimum phase system, that its control is very difficult. The state space equations governing the model are as follows:

$$\dot{x}_{1} = u_{1}\alpha_{1}60(x_{3} - x_{1}) - u_{1}\alpha_{2}60(W_{s} - x_{2}) + \alpha_{3}(Q_{0} - h_{fg}M_{0})$$

$$x_{2} = u_{1}\alpha_{1}60(W_{5} - x_{2}) + \alpha_{4}M_{0}$$

$$\dot{x}_{3} = u_{1}\beta_{1}60(-x_{3} + x_{1}) + u_{1}\beta_{1}15(T_{o} - x_{1}) - u_{1}\beta_{3}60(0.25W_{o} + 0.75x_{2} - W_{s})$$

$$y_{1} = x_{1}$$
(17)

In which the parameters are:

$$u_{1} = f, u_{2} = gpm, x_{1} = T_{3}, x_{2} = W_{3}, x_{3} = T_{2}$$
  

$$\alpha_{1} = 1/V_{s}, \alpha_{2} = h_{fg} / C_{p}V_{s}, \alpha_{3} = 1/\rho C_{p}V_{s},$$
  

$$\alpha_{4} = 1/\rho V_{s}, \beta_{1} = 1/V_{he},$$
  

$$\beta_{2} = 1/\rho C_{p}V_{he}, \beta_{3} = h_{w} / C_{p}V_{he}$$
(18)

Also, the actuator's transfer function can be considered as:

$$G_{act}(S) = k / (l + \tau S)$$
<sup>(19)</sup>

In which k and  $\tau$  are the actuator's gain and time constant. The schematic structure of the HVAC system is given in figure 1. The system has delayed behavior which is represented via linearized, first order and time delay system. Furthermore, the model represents a MIMO system in which one of the I/O channels has a right half plane zero, meaning that it is non-minimum-phase. And the numerical values are given in table 1.

In the first simulation, we compare the results that are taken by using importance factor K1=5 and K2=10

(Multi Agent) with Single Agent controller (K1=5, K2=0).

Table 1. I values for system parameters	
$\rho = .074 \ lb / ft^3$	$C_p = .24 Btu/lb.^{\circ}F$
$V_s = 58464 ft^3$	$T_o = 85^{\circ}F$
$M_o = 166.06  lb  /  hr$	$V_{he} = 60.75 \ ft^3$
$W_s = .007  lb / lb$	$W_o = .0018 \ lb / lb$
$Q_o = 289897$	$\tau = .008 \ hr, \ k = 5$

Table1: Numerical Values for system parameters

The main controller started with random learning coefficient and learning rate ( $\eta$ ) was selected 10 and learning mechanism updated the learning parameters 10 times in a second for each cases. The desired output and Plant output, Control effort and Error are shown in figure 4. As it shown, both of controllers can control and learn the control strategy without any instability and very fast. This on line and fast training

are the most important key points of this method to other one. It is shown that multi agent controller can control the system with less control cost. The maximum of control effort for multi agent controller is 18 but in single agent controller is about 25. So the multi agent controller can be minimized both of error and control effort simultaneously.



Model of the HVAC system



Fig 4 - Comparison of Multi agent controller (k1=5, k2=10) with single agent controller

In the next simulation, we choose k1=5 and k2=5 for multi agent controller. Indeed we expected that the control effort became less than to the last simulation because the importance of second critic agent was increased. This simulation result is shown in fig 5. As we expected the control effort become less than (about 10) the last one but the error become greater than.

### 4. Conclusion

In this paper, we developed a multi agent emotional controller that can achieve to multiple goals and aims.

Online learning, fast convergence, and learning stability are the most important advantages of this controller that are shown in the simulation results. Other important advantage of this method is its robustness and relative independency to plant model that makes it more interesting for real application.

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Fig 5 -Comparison of Multi agent controller (k1=5, K2=5) with single agent controller

Nomenclatures of HVAC System	
$h_w$ Enthalpy of liquid water	$h_{fg}$ Enthalpy of water vapor
$W_s$ Humidity ratio of supply air	$C_p$ Specific heat of air
$M_o$ Moisture load	$T_2$ Temperature of supply air
$V_s$ Volume of thermal space	f Volumetric flow rate of air
$W_o$ Humidity ratio of outdoor air	<i>V<sub>he</sub></i> Volume of heat exchanger
<i>W</i> <sup>3</sup> Humidity ratio of thermal space	$T_o$ Temperature of outdoor air
$Q_o$ Sensible heat load	$T_3$ emperature of thermal space
$\rho$ Air mass density	gpm low rate of chilled water