

## Energy Saving in Electric Trains with Traction Induction Motors

DORU ADRIAN NICOLA<sup>1</sup>      CORNELIA AIDA BULUCEA<sup>1</sup>  
DANIEL CRISTIAN CISMARU<sup>1</sup>      CONSTANTIN BRANDUSA<sup>2</sup>  
GHEORGHE MANOLEA<sup>1</sup>      MARIUS CONSTANTIN POPESCU<sup>1</sup>

<sup>1</sup> Faculty of Electromechanical and Environmental Engineering - University of Craiova

<sup>2</sup> Electrical Vehicles Department ROMDATA AQ Craiova  
ROMANIA

[dnicola@em.ucv.ro](mailto:dnicola@em.ucv.ro) , [abulucea@gmail.com](mailto:abulucea@gmail.com) , [dcismaru@gmail.com](mailto:dcismaru@gmail.com),  
[rinstalctin@yahoo.com](mailto:rinstalctin@yahoo.com), [ghmanolea@gmail.com](mailto:ghmanolea@gmail.com) , [popescu\\_ctin@yahoo.com](mailto:popescu_ctin@yahoo.com)

*Abstract:* The real world processes involving energy and matter need to be linked to the technical and environmental engineering education, design and operation. Energy systems involving conversion chain processes are highly irreversible and, consequently, they could have low exergy efficiencies. In electric railway transportation systems, achieved energy provides a basis for increasing exergy efficiency, reducing both energy losses and environmental damage. Further on, achieved energy modeling can help in optimizing designs and making operating decisions.

*Key-Words:* Electric Transportation, Energy, Environmental Engineering, Exergy, Induction Motor

### 1 Introduction

Scientists and public authorities around the world are realizing that human actions have to be responsible regarding not only the social and economic matters, but also the environment issues. For the moment, our correct activities must be referred into the frame of Sustainable Development. The vitality and perhaps the future survival of the society is strongly depending on the management of physical, environmental and human resources [1]. A dangerously unstable situation is emerging because of people ignorance. The environmental problems are mainly consequences from a too strong belief in traditional engineering and economic growth as the solution [2]. The first human intelligence step against ignorance would be the understanding of concepts such as achieved energy, exergy and embodied energy applied in technical achievements.

On a broader front, an utmost human world priority should be the improvement of public transportation systems. The merit of an electric transportation system is based not only on technical performance, safety, energy efficiency, societal and economic acceptance and but also on environmental impact and exergy efficiency. Costs should reflect value and value is not associated with energy but with achieved energy and exergy [2]. This paper is related to our other studies [3],[4],[5] and aims at establishing the minimum of energy consumption of an electric train on basis of operation analysis at variable frequency with controlled stator flux .

### 2 Transport System with Induction Motors Operating at Variable Frequency and Flux Control

This paper purpose is to demonstrate, as a case study, that the Sustainable Development must be seen and explained as a process which requires both the traditional development analyzation and the further alternatives knowledge. It is taken into account an Electric Transportation System, not simply in terms of technico-economical growth, but also as an achievement of the Sustainable Development. In this study it is understood that the negative effects on efficiency of large exergy destruction and the corresponding longterm environmental degradation can be understood and improved only by an analysis of the transportation systems operation regimes.

The electric trains supplied from a d.c. contact line are equipped with three-phase induction motors (having squirrel cage rotors) and variable voltage and frequency inverters [6]. Since the electric driving systems with static converters and traction induction motors are used, by an appropriate control, with the same electrical machines there can be realized both the traction regime and the electric braking regime of the electric vehicle.

The operation at variable frequency with controlled flux is proceeded to induction motors in drive systems with vectorial control [7]. The vectorial regulation and control method is based on space phasor theory, taking

into consideration the control both of the flux and of the induction machine electromagnetic torque M [8]. As principle, the stator current space phasor is decomposed in two perpendicular components (a flux component and a torque component) which are separately controlled. In this paper will be analyzed the permanent harmonics regime of variable frequency operation with controlled stator flux. It must be noted that in the theoretical achievements it will be taken into account the induction machine with constant parameters, without iron losses or saturation.

The three-phase induction machine equations (with phase quantities) depending on stator flux  $\psi_s$  are specified by the system (1) and correspondingly to the operation with  $\psi_s = ct.$  and  $\omega_s = var.$ , the phase equivalent scheme of induction machine [9] is presented in Fig.1.

$$\begin{aligned} \underline{U}_s &= R_s \underline{I}_s + j \omega_s \underline{\Psi}_s \\ 0 &= \frac{\omega_s}{\omega_r} R_r' \left(\frac{L_s}{L_u}\right)^2 \left(\frac{L_u}{L_s} \underline{I}_{r'}\right) + \\ &+ j \omega_s \frac{\sigma L_s}{1-\sigma} \left(\frac{L_u}{L_s} \underline{I}_{r'}\right) + \omega_s \underline{\Psi}_s \end{aligned} \quad (1)$$

$$\underline{\Psi}_s = L_s \underline{I}_{ms}$$

$$\underline{I}_{ms} = \underline{I}_s + \frac{L_u}{L_s} \underline{I}_{r'}$$

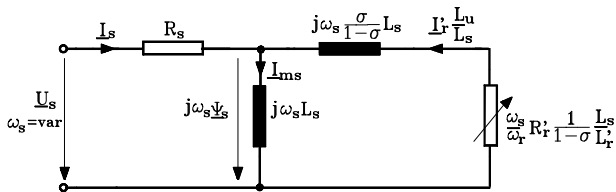


Fig.1 Equivalent scheme at  $\psi_s=ct.$  and  $\omega_s=var.$

Because of  $\psi_s = L_s \cdot I_{ms}$  it means that the stator flux  $\psi_s$  control is reducing actually at the magnetizing current  $I_{ms}$  control. On the other hand, the equivalent scheme presented in Fig.1 allows the currents equation written as below:

$$\underline{I}_s = \underline{I}_{ms} + \left(-\underline{I}_{r'} \frac{L_u}{L_s}\right) \quad (2)$$

where:

$$\begin{aligned} \underline{I}_{ms} &= \frac{\underline{\psi}_s}{L_s} \\ -\underline{I}_{r'} \cdot \frac{L_u}{L_s} &= \frac{\underline{\psi}_s}{L_s} \cdot \frac{j}{\frac{\sigma}{1-\sigma} L_s \frac{R_r'}{\omega_r \sigma L_r'} + j} \end{aligned} \quad (3)$$

It means that within condition  $\psi_s = ct.$  the effective value  $I_s$  of stator current is not depending on the

supply voltage (or current) frequency  $f_s = \omega_s / (2\pi)$ .

Analytically, in the complex frame (+1, +j), with the real axis along the phasor  $\underline{\psi}_s$  (thus, with  $\underline{\psi}_s = \psi_s + j0$ ), the stator current will be:

$$\begin{aligned} \underline{I}_s &= \frac{\underline{\psi}_s}{L_s} + \frac{\underline{\psi}_s}{\frac{\sigma}{1-\sigma} L_s} \cdot \frac{j}{\frac{R_r'}{\omega_r \sigma L_r'} + j} = \\ &= I_{sx} + j \cdot I_{sy} \end{aligned} \quad (4)$$

The stator current phasor diagram  $\underline{I}_s$  is presented in Fig.2 [6].

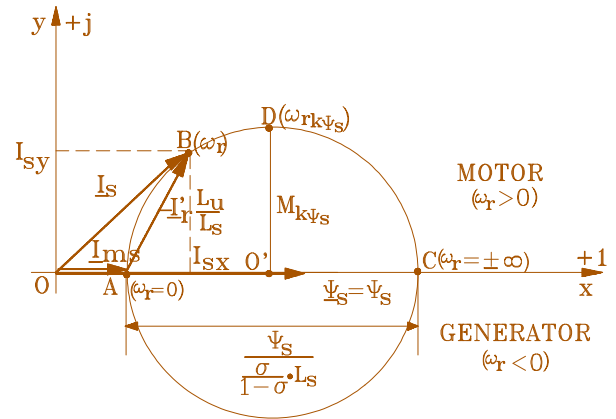


Fig.2 Stator current phasor  $\underline{I}_s$  at  $\psi_s=ct.$  and  $\omega_r=var.$

It is obviously that when  $\psi_s = ct.$  and  $\omega_r = var.$ , the component  $-\underline{I}_{r'} \cdot (L_u/L_s)$  of stator current  $\underline{I}_s$  is variable in phase and magnitude, so that the point B will describe the circle ADC with diameter  $AC = (1-\sigma)\psi_s / (\sigma L_s) = constant$ . Due to the constant value of the stator current component  $I_{ms}$ , it means that the same circle will be describe by the phasor  $\underline{I}_s$  when the flux  $\psi_s = ct.$  and the pulsation  $\omega_r = var.$

The mathematics calculus allows for the stator current components the relations as following:

$$\begin{aligned} I_{sx} &= \frac{\psi_s}{L_s} + \frac{1-\sigma}{\sigma L_s} \frac{\psi_s}{\frac{R_r'}{\omega_r \sigma L_r'} + \frac{\omega_r \sigma L_r'}{R_r'}} \\ I_{sy} &= \frac{1-\sigma}{\sigma L_s} \frac{\psi_s}{\frac{R_r'}{\omega_r \sigma L_r'} + \frac{\omega_r \sigma L_r'}{R_r'}} \end{aligned} \quad (5)$$

The stator current absolute value can be determined by formula  $I_s = (I_{sx}^2 + I_{sy}^2)^{1/2}$ .

Electromagnetic torque M in complex coordinates axes system (oriented on  $\underline{\psi}_s$ ) is:

$$\begin{aligned} M &= 3p \cdot \text{Im}\{\underline{I}_s \cdot \underline{\psi}_s^*\} = \\ &= 3p \cdot \text{Im}\{(I_{sx} + jI_{sy}) \cdot \psi_s\} = \\ &= 3p \cdot \psi_s \cdot I_{sy} \end{aligned} \quad (6)$$

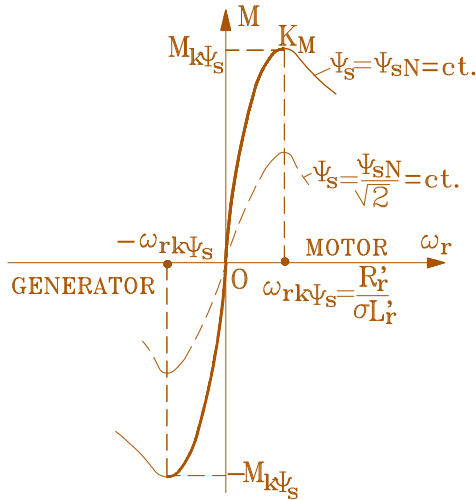


Fig.3 Torque characteristic  $M=f(\omega_r)$  at controlled stator flux

Replacing  $I_{sy}$  from (5), the torque  $M$  relation becomes:

$$M = 3p \cdot \frac{1 - \sigma}{\sigma L_s} \cdot \frac{\psi_s^2}{\frac{R_r'}{\omega_r \sigma L_r'} + \frac{\omega_r \sigma L_r'}{R_r'}} \quad (7)$$

When stator flux is constant ( $\psi_s=ct.$ ) then electromagnetic torque magnitude depends on rotor currents pulsation  $\omega_r$  and doesn't depend on stator supply frequency  $f_s$ . The torque curve  $M = f(\omega_r)$  at  $\psi_s = ct.$  will not linearly depend on  $\omega_r$ , having two symmetrical extremes, as below:

$$\frac{\partial M}{\partial \omega_r} = 0; \quad \omega_{rk\psi_s} = \pm \frac{R_r'}{\sigma \cdot L_r'}; \quad (8)$$

$$M_{k\psi_s} = M(\omega_{rk\psi_s}) = \pm \frac{3p}{2} \cdot \frac{1 - \sigma}{\sigma \cdot L_s} \cdot \psi_s^2$$

The graphical dependence  $M = f(\omega_r)$  at  $\psi_s = ct.$  is represented in Fig.3.

In motor regime, taking into account the coordinates of maxima point  $K_M$ , the relation (7) can be achieved as "Kloss formula":

$$M = \frac{2M_{k\psi_s}}{\frac{\omega_r}{\omega_{rk\psi_s}} + \frac{\omega_{rk\psi_s}}{\omega_r}} \quad (9)$$

In steady-state regime, a stable operation (with  $\partial M/\partial \omega_r > 0$ ) is performed only on the ascendent zone of the characteristic  $M = f(\omega_r)$  presented in Fig.3 and it is corresponding at small rotor pulsations, according the condition  $|\omega_r| \leq \omega_{rk\psi_s}$ . Mechanical characteristics family  $M = f(n)$  of induction motor operating at  $\psi_s=ct.$ , for different constant values of stator frequency ( $f_s = ct.$ ) are shown in Fig.4.

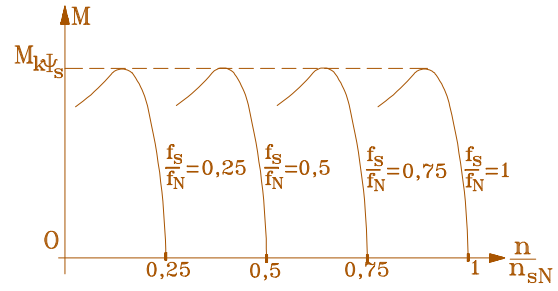


Fig.4 Mechanical characteristics  $M=f(n)$  at  $\psi_s=ct.$  for different frequency  $f_s$  values ( $f_s \leq f_N$ )

These characteristics had been drawn on basis of relation (9), taking into account that, to any value of frequency  $f_s = \omega_s/(2\pi)$ , it will result  $\omega_r = \omega_s - \omega_m$  with  $\omega_m = p \cdot \Omega_m = p \cdot 2\pi n/60$ .

The constant stator flux magnitude ( $\psi_s=ct.$ ) to any stator frequency  $f_s$  value and to torque  $M$  (respectively, any rotor pulsation  $\omega_r$ ) impose an exact control either of the supply voltage  $U_s$  or of supply current  $I_s$ .

As magnitude, the stator voltage  $U_s$  effective value results from the electric equivalent presented in Fig.1. When  $\psi_s = ct.$  the voltage  $U_s$  will depend on both  $\omega_s$  and  $\omega_r = \omega_s - \omega_m$ .

Absolutely similar, the stator current  $I_s$  at constant stator flux ( $\psi_s=ct.$ ) can be expressed as depending on  $\omega_r$  or on electromagnetic torque  $M$ . As dependence of electromagnetic torque  $M$ , with  $\omega_r \cdot \sigma \cdot L_r'/R_r'$  from (6), as below:

$$\frac{\omega_r \sigma L_r'}{R_r'} = \frac{M_{k\psi_s}}{M} \cdot \sqrt{\left(\frac{M_{k\psi_s}}{M}\right)^2 - 1} \quad (10)$$

there will be obtained the two components  $I_{sx}$  and  $I_{sy}$  of stator current  $I_s$ :

$$I_{sx} = \frac{\psi_s}{L_s} + \frac{\psi_s}{L_s} \frac{1 - \sigma}{2\sigma} \left[ 1 - \sqrt{1 - \left(\frac{M}{M_{k\psi_s}}\right)^2} \right]$$

$$I_{sy} = \frac{M}{3p\psi_s} = \frac{\psi_s}{L_s} \frac{1 - \sigma}{2\sigma} \frac{M}{M_{k\psi_s}} \quad (11)$$

Consequently, at constant stator flux ( $\psi_s = ct.$ ), the effective value of stator current  $I_s = (I_{sx}^2 + I_{sy}^2)^{1/2}$  will depend on electromagnetic torque  $M$  according to relation:

$$I_s = \frac{\psi_s}{L_s} \sqrt{\left[ \frac{1 - \sigma}{2\sigma} - \frac{1 - \sigma}{2\sigma} \sqrt{1 - \left(\frac{M}{M_{k\psi_s}}\right)^2} \right]^2 + \left[ \frac{1 - \sigma}{2\sigma} \frac{M}{M_{k\psi_s}} \right]^2} \quad (12)$$

### 3 Variation Range of Stator Frequency

When the supply voltages (or currents) are with variable frequency, it is important to establish the limit values, meaning the minimum frequency  $f_{smin}$  and the maximum frequency  $f_{smax}$  of the stable operation range of the induction machine.

#### 3.1 Minimum Frequency at Constant Stator Flux Operation

In steady-state regime, to any stator frequency value  $f_s$ , among the pulsation  $\omega_r$ ,  $\omega_s = 2\pi \cdot f_s$  and  $\omega_m = p \cdot \Omega_m = p \cdot 2\pi \cdot n / 60$ , according to *Frequencies Theorem* it is true the relation as below:

$$\omega_s = \omega_m + \omega_r \tag{13}$$

Consequently, for any given value of stator frequency  $f_s$  and rotor pulsation  $\omega_r$ , respectively, it will be possible to establish the steady-state rotor speed  $n$ :

$$2\pi f_s = p \frac{2\pi n}{60} + \omega_r$$

$$\Rightarrow n = \frac{60}{p} \left( f_s - \frac{1}{2\pi} \omega_r \right) \tag{14}$$

If the normal operation at the frequency  $f_s$  is proceeding with constant stator flux  $\Psi_s = \Psi_{sN} = ct.$ , then the speed  $n_k$  corresponding to the maximum electromagnetic torque  $M$  (see the point  $K_M$  in Fig.5)) will be calculated as following:

$$n_k = \frac{60}{p} \left( f_s - \frac{1}{2\pi} \omega_{rk\psi_s} \right)$$

$$n_k \geq 0 \tag{15}$$

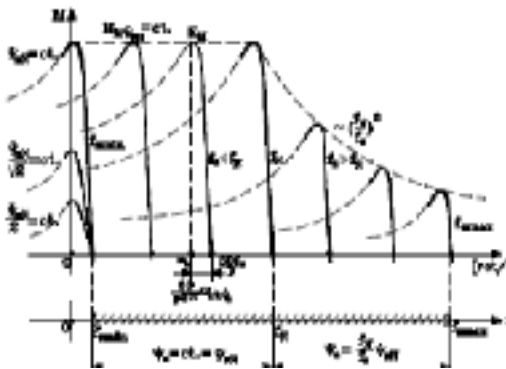


Fig.5 Stator frequency  $f_s$  extreme values

Hence, the minimum stator frequency  $f_{smin}$  which makes possible the operation conditions as before will correspond to the limit case when  $n_k = 0$ , resulting  $f_{smin}$ :

$$f_{smin} = \frac{1}{2\pi} \omega_{rk\psi_s} = \frac{1}{2\pi} \frac{R_r'}{\sigma L_r'} \tag{16}$$

This is the minimum frequency value which must be provided by the supply source. It is depending on

induction machine parameters  $R_r'$ ,  $L_r'$  and  $\sigma$ .

Also, in Fig.5 it is emphasized the slide starting method, by a progressive increase of stator flux  $\Psi_s$  from 0 to  $\Psi_{sN}$  (at the minimum value  $f_{smin} = ct.$  of supply stator frequency).

#### 3.2 Maximum Frequency at Operation with Weaken Stator Flux

In the over-rated frequency range  $f_s > f_{sN}$ , because of the stator voltage limitation at  $U_s = U_N$ , the induction machine will operate in weaken stator flux conditions. Normally, the stator flux  $\Psi_s$  decrease is proceeding by the law " $1/\omega_s$ " written as below:

$$\psi_s = \psi_{sN} \frac{\omega_N}{\omega_s} = \frac{U_N}{\omega_s} \tag{17}$$

As result, the decrease of flux  $\Psi_s$  will determine a loss in capability of maximum torque  $M_{k\psi_s}$  which at  $f_s > f_{sN}$  becomes:

$$M_{k\psi_s} = \frac{3p}{2} \frac{1 - \sigma}{\sigma L_s} \left[ \psi_{sN} \frac{\omega_N}{\omega_s} \right]^2$$

$$= M_{k\psi_{sN}} \left( \frac{\omega_N}{\omega_s} \right)^2 \tag{18}$$

Consequently, the electromagnetic torque  $M$  determined at  $\omega_r = ct.$  and  $f_s > f_{sN}$  will decrease in the same ratio. Graphically, in the right side of Fig.6 there are represented three mechanical characteristics  $M=f(n)$  at decreased flux according to the law  $\Psi_s = \Psi_{sN} \cdot \omega_N / \omega_s$  and  $f_s = ct.$  (with  $f_s > f_{sN}$ ).

In that framework, the stator frequency maximum value  $f_{smax}$  will be established from the invariant electromagnetic power condition  $P_M = M \cdot \Omega_s = M \cdot \omega_s / p$  for different stator frequency values  $f_s$ . Hence, in the aim to ensure  $P_M = ct.$  in the range of limit frequencies  $f_{sN}$  and  $f_{smax}$  it is compulsory that:

$$M_N \frac{\omega_N}{p} = M_{f_{smax}} \frac{\omega_{smax}}{p} \tag{19}$$

If at the maximum stator frequency  $f_{smax}$  it is imposed the condition  $M_{f_{smax}} = M_{k\psi_s}$ , where  $M_{k\psi_s}$  is determined by (18), then we will obtain:

$$M_N \cdot \frac{\omega_N}{p} = M_{k\psi_{sN}} \cdot \left( \frac{\omega_N}{\omega_{smax}} \right)^2 \cdot \frac{\omega_{smax}}{p}$$

$$\Rightarrow \omega_{smax} = \frac{M_{k\psi_{sN}}}{M_N} \cdot \omega_N \tag{20}$$

or:

$$\lambda_M = \frac{M_{k\psi_{sN}}}{M_N}$$

$$\Rightarrow f_{smax} = \lambda_M \cdot f_N \tag{21}$$

Hence, the increase of frequency  $f_{smax}$  could be obtained only by designing an induction machine with an increased overload torque capability  $\lambda_M$ . It is compulsory to be noticed that for the normal induction machines  $\lambda_M = 2,2 \dots 2,5$ .

Consequently, when we are taken into account the induction machine operation with variable stator frequency, there must be emphasized that the supply voltage (or current) frequency minimum  $f_{smin}$  and maximum  $f_{smax}$  values are depending only on that induction machine parameters.

### 4 Energy Saving in Train Operation

In the power schemes of electric trains, the traction induction motor represents the final element in the conversion energy equipments chain [3]. After all, it achieves the electromechanical conversion of energy making thus possibly the movement. For an achieved energy dynamic approach both of the traction motor and of the useful movement mathematical models are necessary. Further on, there will be achieved the structural diagrams [4], so that, by an appropriate train control, the minimum of energy consumption will be obtained.

As a complex electromechanical system, the induction motor could be conceptually decomposed into an electromagnetic subsystem and a mechanical subsystem. Between these two functional parts, both the electromagnetic torque  $M$  and the rotor mechanical speed  $\Omega_m$  are interacting as internal variables. The induction motor electromagnetic part will be described by the equations [5]:

$$\frac{d\psi_s}{dt} = \underline{u}_s - R_s \cdot \underline{i}_s$$

$$\frac{d\psi_r'}{dt} = j \cdot p \cdot \Omega_m \cdot \underline{\psi}_r' - R_r' \cdot \underline{i}_r' \tag{22}$$

$$\underline{i}_s = \frac{\underline{\psi}_s - \frac{L_u}{L_r'} \cdot \underline{\psi}_r'}{\sigma L_s}; \quad \underline{i}_r' = \frac{\underline{\psi}_r' - \frac{L_u}{L_s} \cdot \underline{\psi}_s}{\sigma L_r'}$$

$$M = \frac{3}{2} \cdot p \cdot \text{Im} \{ \underline{i}_s \cdot \underline{\psi}_s^* \}$$

where:  $\underline{u}_s$  is the stator voltage vector;  $\underline{i}_s$  is the stator current vector;  $\underline{i}_r'$  is the rotor current vector;  $\underline{\psi}_s$  is the stator flux vector;  $\underline{\psi}_r'$  is the rotor flux vector;  $L_u$  is the magnetizing inductance;  $L_s$  is the stator inductance;  $L_r'$  is the rotor inductance;  $p$  is number of pole pairs;  $R_s$  is the stator resistance;  $R_r'$  is the rotor resistance and  $\sigma = 1 - \frac{L_u^2}{L_s \cdot L_r'}$  is the motor leakage coefficient.

On basis of equations (22) the structural diagram and the mask block of the induction motor electromagnetic part are represented in Fig.6, a. The

structural diagram of electromagnetic subsystem can be coupled both with the structural diagram of machine converter through the input variables  $\underline{u}_s$  and output variables  $\underline{i}_s$  and with the structural diagram of mechanical part through input quantities  $\Omega_m$  and output quantities  $M$ . In Fig.7 the structural diagram of useful moment is presented.

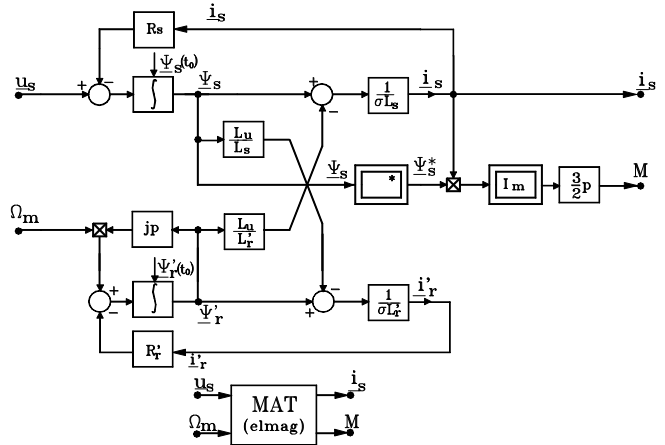


Fig.6 Structural diagram and mask block for electromagnetic part of induction motor

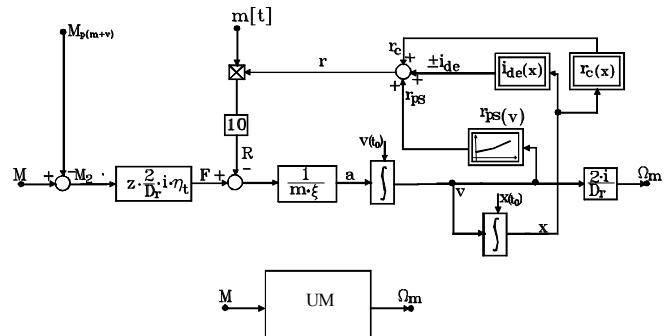


Fig.7 Structural diagram and mask block of useful movement

The next step of train operation achieved energy analysis encompass the numerical simulations of different train operation regimes. Hence, the validity and trustfulness of the achieved mathematical models and structural diagrams had been verified by simulations of traction induction motor regimes.

In Fig.8 the SIMULINK – SimPowerSystems Model [10] for traction motors (MABT1, MABT2 and MABT3) transient starting regime simulation is presented, and on this basis, in Fig.9 there are presented the simulations of phase current and speed in the transient starting regime of traction induction motor supplied at variable voltage and frequency source  $n^* = 1135 \text{ rot/min}$  ( $\omega^* = 118,9 \text{ rad/s}$ ). Further on, the simulation and test results (Fig.10) were compared in order to establish the match.

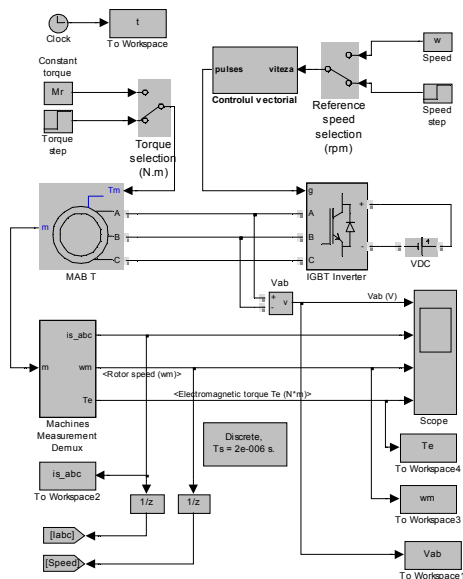


Fig.8 SIMULINK – SimPowerSystems Model for study of traction induction motors supplied at variable voltage and frequency source

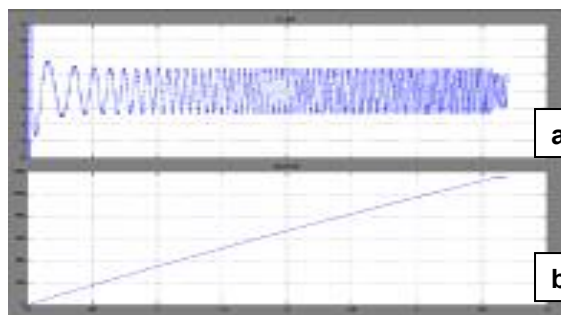


Fig.9 Transient starting regime simulation of traction induction motor supplied at variable voltage and frequency source  $n^* = 1135 \text{ rot/min}$  ( $\omega^* = 118,9 \text{ rad/s}$ )  
a) Phase current; b) Speed

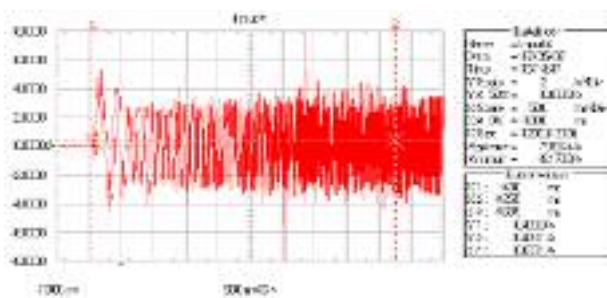


Fig.10 Transient starting regime test of traction induction motor supplied at variable voltage and frequency source  $n^* = 1135 \text{ rot/min}$  ( $\omega^* = 118,9 \text{ rad/s}$ )

## 5 Conclusions

The real world processes involving energy and matter need to be linked to the environmental engineering education, design and operation. Energy systems involving conversion chain processes are highly irreversible and, consequently, they could

have low exergy efficiencies. This observation also implies that there is great potential for improving the performance of such systems. This paper emphasizes the achieved energy analysis, related as tool in order to describe, analyse and optimize energy conversion in electric railway transportation systems. This way, it could be obtained a high exergy efficiency, due to the matching of simulation and experimental data. In traction regime, the electric trains accomplishes remarkable results. Using the structural diagrams and high techniques converters, an appropriate vehicle control can be achieved. The power converters and the efficient anti-skidding systems have ensured the optimum traction characteristics and a minimum of energy consumption.

In a longterm, the important application of this research is to address sustainability issues in a qualitative and quantitative fashion through a complete analysis of the electric railway transportation systems.

## References:

- [1] Wall G (1994). *Exergy, Ecology and Democracy – Concepts of a Vital Society or A proposal for An Exergy Tax*, the 2<sup>nd</sup> European Congress on Economics and Management of Energy in Industry, Estoril, Portugal, April 5-9.
- [2] Dincer I. and Rosen M.A. (2007), *Exergy: Energy, Environment and Sustainable Development*, Oxford, UK: Elsevier.
- [3] Bulucea C.A., Nicola D.A., Brandusa A., Brandusa C. (2008), *Drive Systems in Underground Metro Saving Energy*, 3<sup>rd</sup> IASME/WSEAS Int. Conference on ENERGY & ENVIRONMENT (EE'08), University of Cambridge, UK, February 23-25, pp.433-439.
- [4] Bulucea C.A., Brandusa C., Cismaru D., Nicola D.A. (2008) *Energy and Exergy Efficiencies in Urban Electric Transportation Systems*, WSEAS TRANSACTIONS on ENVIRONMENT and DEVELOPMENT, Issue 3, Volume 4, March, ISSN 1790-5079, pp.247-259.
- [5] Cismaru D.C., Nicola D.A., Manolea G., Drighiciu A., Bulucea C.A. (2008), *Mathematical Models of High-Speed Trains Movement*, WSEAS TRANSACTIONS on CIRCUITS and SYSTEMS, Issue 2, Volume 7, February, ISSN 1109-2734, pp379-388.
- [6] Nicola D.A. Cismaru D.C. (2006) *Tractiune Electrica: Fenomene, Modele, Solutii*, Ed. SITECH Craiova, Romania.
- [7] Buhler H. (1997), *Reglage de Systemes d'Electronique de Puissance*, Vol.I, PPUR, Lausanne.
- [8] Klima J. (2006). *An Analytical Model and Investigation of Induction Motor Drive Fed from Three-Level Space-Vector Modulated VSI*, Proceedings of 6<sup>th</sup> WSEAS/IASME International Conference on ELECTRIC POWER SYSTEMS, HIGH VOLTAGES, ELECTRIC MACHINES (POWER'05), Tenerife, Spain, December 2006.
- [9] Jamoussi K., Ouali M., Charradi H. (2007), *A Sliding Mode Speed Control of an Induction Motor*, WSEAS TRANSACTIONS on SYSTEMS and CONTROL, Issue 7, Volume 2, July 2007, ISSN 1991-8763, pp379-388.
- [10] Brandusa C (2007)., *Driving Systems with Static Converters and Induction Motors in Electric Urban Traction*, Ph.D. Thesis, Univ Petrosani, Romania.